

MVE045 W3-RÖ1 (relevanta problem)

kedjeregeln, implicit derivata

ADAMS 2.1

In Exercises 1–12, find an equation of the straight line tangent to the given curve at the point indicated.

1. $y = 3x - 1$ at $(1, 2)$

2. $y = x/2$ at $(a, a/2)$

3. $y = 2x^2 - 5$ at $(2, 3)$

4. $y = 6 - x - x^2$ at $x = -2$

5. $y = x^3 + 8$ at $x = -2$

6. $y = \frac{1}{x^2 + 1}$ at $(0, 1)$

20. Find all points on the curve $y = x^3 - 3x$ where the tangent line is parallel to the x -axis.

24. For what value of the constant k do the curves $y = kx^2$ and $y = k(x - 2)^2$ intersect at right angles? *Hint:* Where do the curves intersect? What are their slopes there?

ADAMS 2.2

In Exercises 11–24, (a) calculate the derivative of the given function directly from the definition of derivative, and (b) express the result of (a) using differentials.

11. $y = x^2 - 3x$

12. $f(x) = 1 + 4x - 5x^2$

13. $f(x) = x^3$

14. $s = \frac{1}{3 + 4t}$

Calculate the derivatives of the functions in Exercises 34–39 using the General Power Rule. Where is each derivative valid?

34. $f(x) = x^{-17}$

35. $g(t) = t^{22}$

36. $y = x^{1/3}$

37. $y = x^{-1/3}$

ADAMS 2.4 kedjeregeln med polynom och rationella funktioner

THEOREM

6

The Chain Rule

If $f(u)$ is differentiable at $u = g(x)$, and $g(x)$ is differentiable at x , then the composite function $f \circ g(x) = f(g(x))$ is differentiable at x , and

$$(f \circ g)'(x) = f'(g(x))g'(x).$$

Find the derivatives of the functions in Exercises 1–16.

1. $y = (2x + 3)^6$

2. $y = \left(1 - \frac{x}{3}\right)^{99}$

3. $f(x) = (4 - x^2)^{10}$

4. $y = \sqrt{1 - 3x^2}$

5. $F(t) = \left(2 + \frac{3}{t}\right)^{-10}$

6. $(1 + x^{2/3})^{3/2}$

? 9. $y = |1 - x^2|$

ADAMS 2.8 medelvärdesatsen

THEOREM

11

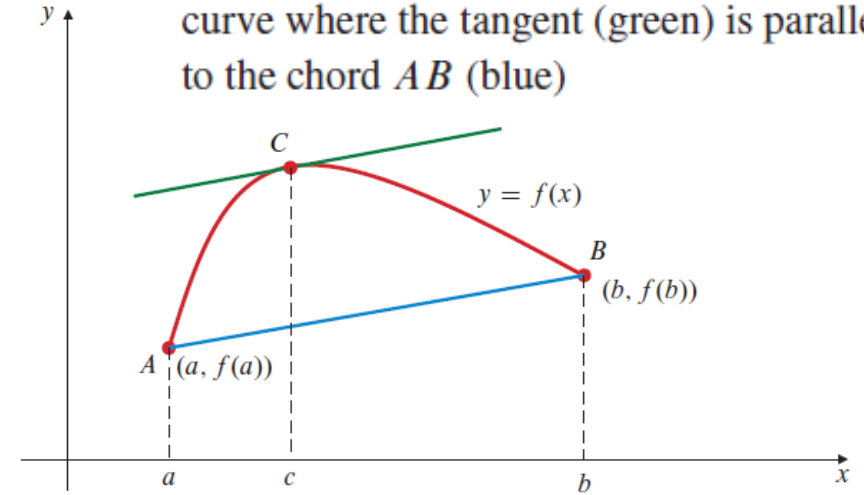
The Mean-Value Theorem

Suppose that the function f is continuous on the closed, finite interval $[a, b]$ and that it is differentiable on the open interval (a, b) . Then there exists a point c in the open interval (a, b) such that

$$\frac{f(b) - f(a)}{b - a} = f'(c).$$

This says that the slope of the chord line joining the points $(a, f(a))$ and $(b, f(b))$ is equal to the slope of the tangent line to the curve $y = f(x)$ at the point $(c, f(c))$, so the two lines are parallel.

Figure 2.28 There is a point C on the curve where the tangent (green) is parallel to the chord AB (blue)



In Exercises 1–3, illustrate the Mean-Value Theorem by finding any points in the open interval (a, b) where the tangent line to $y = f(x)$ is parallel to the chord line joining $(a, f(a))$ and $(b, f(b))$.

1. $f(x) = x^2$ on $[a, b]$
2. $f(x) = \frac{1}{x}$ on $[1, 2]$
3. $f(x) = x^3 - 3x + 1$ on $[-2, 2]$