

The density above is

 $\pi(\theta) = 0.3 \cdot \text{Normal}(\theta; 2, 0.5^2) + 0.7 \cdot \text{Normal}(\theta; 6; 1^2)$. It is easy to directly obtain a sample from this density, but below, we will use MCMC.

- (a) Program in R a Random Walk Metropolis Hastings algorithm to derive an approximate sample from the density above. Use as proposal $\theta^* = \theta_{i-1} + \epsilon$ where $\epsilon \sim \text{Uniform}(-0.5, 0.5)$. Use the sample to approximate the expectation of the density above.
- (b) Is your approximation accurate? How can you check whether it is accurate? What can you change in the algorithm above to get better accuracy?