# Some exercises week 1 MSA101/MVE187 autumn 2021 

Petter Mostad

September 1, 2021

1. Tests with the outcomes "success" or "failure" are done, each with a probability of success $\theta$, and their outcomes are indpendent given $\theta$. The prior for $\theta$ is uniform on the interval from zero to one. Assume 5 tests are done, and 4 are successful. What is the posterior for $\theta$ given this information? What is the probability that $\theta$ is 0.8 or more?
2. Each day, a count of some rare birds are made. We assume the counts are Poisson distributed with parameter $\lambda$, and that they are independent given $\lambda$. The prior for $\lambda$ is $\operatorname{Gamma}(3,1)$
(a) In three consecutive days, 5,7 , and 4 birds are counted. What is the posterior for $\lambda$ given this information?
(b) What is the predictive probability distribution for the number of birds that will be counted on the fourth day? What is the probability that at least 5 birds will be counted?
3. We assume observations are sampled from a normal distribution $\operatorname{Normal}(3,1 / \tau)$, where $\tau$ has a $\operatorname{Gamma}(2,2)$ prior. The values observed are 3.5, 4.1, and 2.3.
(a) Find the posterior distribution for $\tau$ given the data.
(b) Find the probability density for the predictive distribution for the next observation that is sampled from the distribution. Can you recognize this as a distribution in a named family of distributions?
