

Financial Risk 4-th quarter 2020/21 Lecture 4: Dependence, backtesting

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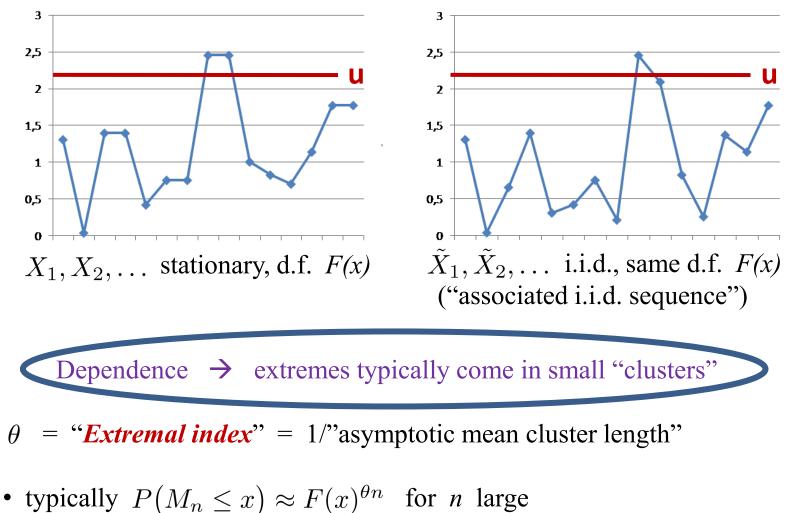


"As an alternative to the traditional 30-year mortgage, we also offer an interest-only mortgage, balloon mortgage, reverse mortgage, upside down mortgage, inside out mortgage, loop-de-loop mortgage, and the spinning double axel mortgage with a triple lutz."



Gudrun January 2005 326 MEuro loss 72 % due to forest losses 4 times larger than second largest

#### **Dependence: Extreme Value Statistics for stationary time series** (Coles p. 92-104)



- typically clusters asymptotically i.i.d., dependence within clusters
- typically tail of cluster maxima asymptotically same as  $\bar{F}(x)$  !!
- typically the GEV distributions the only possible limit distributions

## The block maxima method for stationary time series

If blocks are sufficiently long, then block maxima (typically) are approximately independent, and one can use Extreme Value Statistics in precisely the same way as for i.i.d. sequences

## The PoT method for stationary time series

- **1. Decluster:** identify approximately i.i.d clusters of large values by a) Block method: divide observations up into blocks of a fixed length r, all values in a block which exceed the level *u* is a cluster
  - b) Blocks-runs method: the first cluster starts at first exceedance of u and contains all excesses of u within a fixed length r thereafter. The second cluster starts at the next exceedance of *u* and contains all excesses of *u* within *r* thereafter, and so on...
  - c) Runs method: the first cluster starts with the first exceedance of u and stops as soon as there is a value below *u*, the second cluster starts with the next exceedance of *u*, and so on ...
- 2.  $\hat{\theta} = \frac{\text{no. of clusters}}{\text{no. of exceedances}}$  estimate of the *extremal index*

- 3. PoT: Use standard i.i.d. PoT model, but with excesses replaced by cluster maxima, and excedance times replaced by the times when cluster maxima occur. (A bit of a miracle this works. Proof not given here.)
- **4.** Use  $P(M_n \le x) \approx F(x)^{\theta n}$  to switch between block maxima and PoT

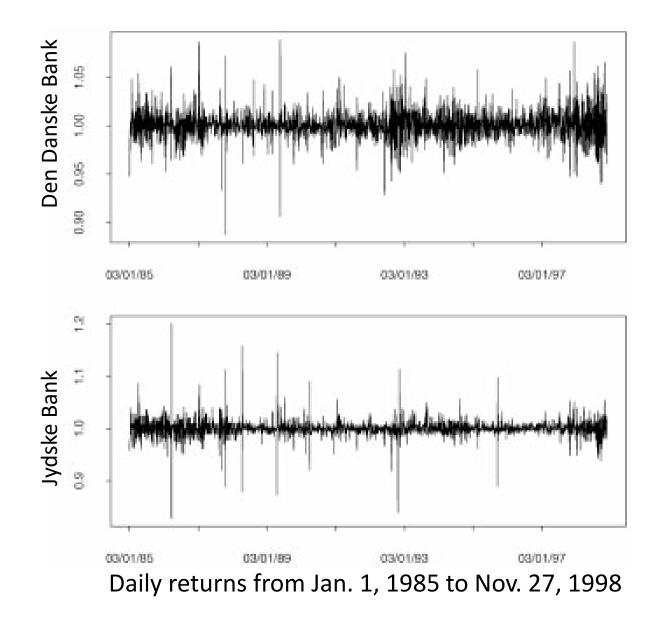
## Estimating value at risk by extreme value methods;

(Sarah Lauridsen, Extremes 3, 107-144, 2000)

VaR = high quantiles of the loss-profits distribution

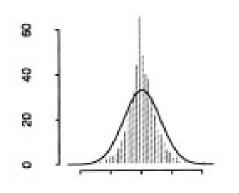
- empirical quantiles
- unconditional Gaussian method
- conditional Gaussian method
- GEV + different extremal index estimators
- GP pretending independence
- GP with declustering
- GARCH + GP residuals, conditional
- GARCH + GP residuals, unconditional

#### Compared, and evaluated via backtesting

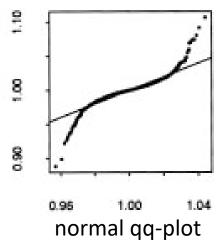


Synthetic portfolio: 50 MDKK Danske Bank + 50 MDKK Jydske Bank

#### **Empirical and Normal**



histogram with estimated normal density (13 left values and 10 right values not shown)



VaR in mDKr estimated by Gaussian and empirical method								
1-day VaR	95%	96%	97%	98%	99%	99.9%	99.99%	
Gaussian method	1.93	- 2.05	- 2.21	2.42	- 2.75	3.67	- 4.42	
Empirical method	1.66	- 1.85	- 2.07	2.43	- 3.10	7.55		

To assume returns normally distributed and i.i.d. gives easy calculations, also for complex portfolios

-- but, distribution doesn't fit in the tails, independence not OK

-- the empirical method gives no estimates for extreme quantiles

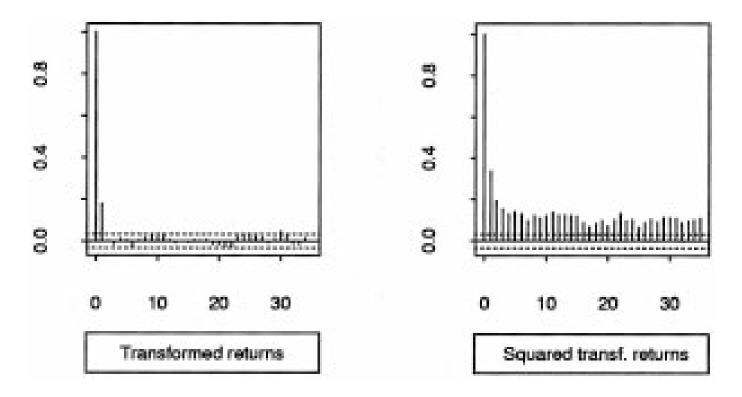
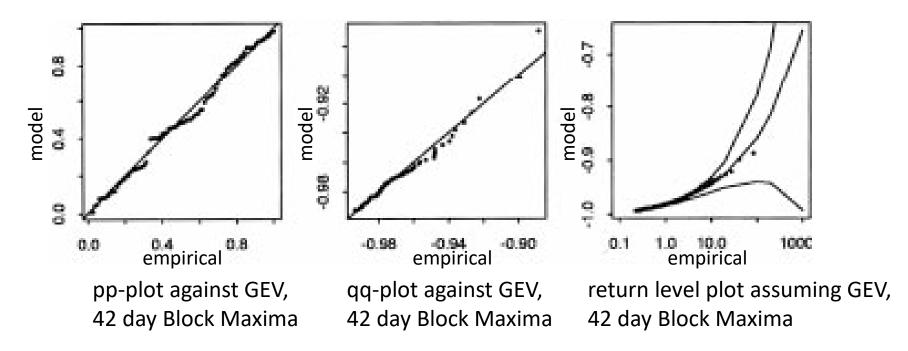


Figure 3. Auto correlograms for the searce of daily returns on the bank positions. The returns have been transformed to have Gaussian marginals.

checked dependence by transforming to normal marginal distribution and computing correlations  $\rightarrow$  clear and strong dependence

Block Maxima for 42 days approximately independent (figure not shown)

#### **Block Maxima**



GEV distribution fits the data well, and 42 days maxima interesting for firm survival, but how can one get from there to overnight VaR?

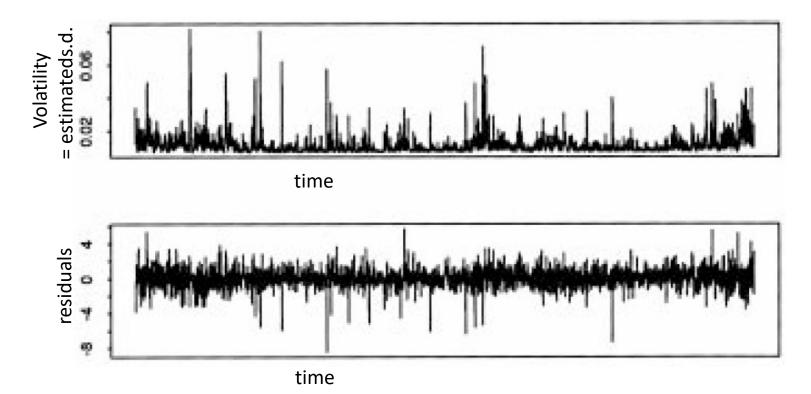
 $\alpha$ - quantile of overnight P&L-distribution estimated by  $\alpha^{n\theta}$ - quantile of n-day maxima

- But  $\theta$  difficult to estimate

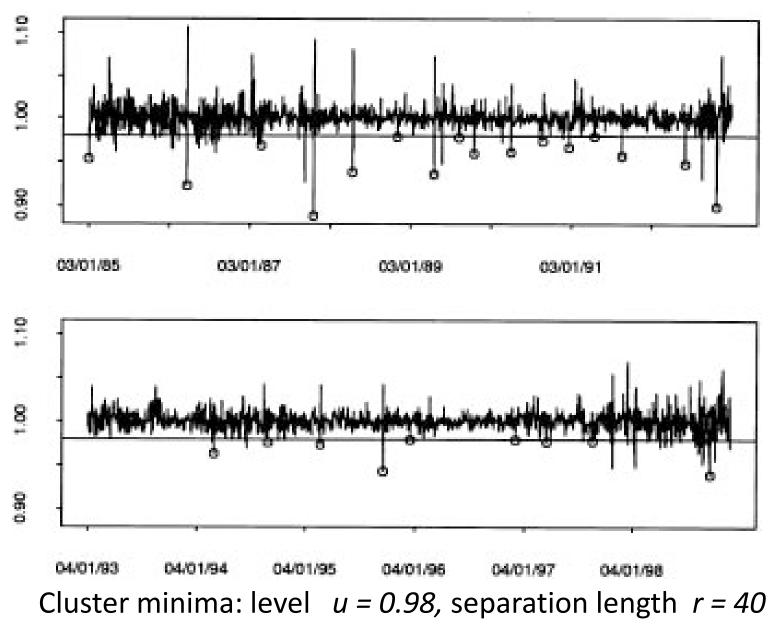
## Garch

fit Garch model, compute residuals, fit GP distribution to residuals, compute quantiles of the resulting estimated distribution of returns (computation done by simulation).

Can be done *conditionally*, using volatility today to compute quantiles for the portfolio tomorrow or *unconditionally* – for longrun behaviour of portfolio



PoT



$ \begin{array}{c c c c c c c c c c c c c c c c c c c $		Backtesting results, violations of 1-day VaR Empirical method								
$\begin{array}{c} & & & & & & & & & & & & & & & & & & &$		95%	96%	97%	98%	99%	99.9%	99.99%		
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	Portfolio	119 (99.3)	100 (79.4)	74 (59.6)	56 (39.7)	30 (19.9)	1 (2.0)	- (0.2)		
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	S&P 500	101 (159.9)	77 (127.9)	55 (95.9)	35 (64.0)	20 (32.0)	3 (3.2)	- (0.3)		
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	B&O		72 (79.4)		35 (39.7)			- (0.2)		
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	Carlsberg	81 (99.3)	68 (79.4)	56 (59.6)	39 (39.7)	17 (19.9)	0 (2.0)	- (0.2)		
Novo B     113 (99.3)     90 (79.4)     70 (59.6)     49 (39.7)     26 (19.9)     2 (2.0)     - (0.2       Svendborg     122 (99.3)     96 (79.4)     77 (59.6)     55 (39.7)     30 (19.9)     4 (2.0)     - (0.2       Unconditional Gaussian method       Unconditional Gaussian method       See 500     101 (159.9)     79 (127.9)     59 (95.9)     36 (64.0)     22 (32.0)     5 (3.2)     3 (0.3)       B&O     61 (99.3)     55 (79.4)     49 (59.6)     40 (39.7)     28 (19.9)     13 (2.0)     9 (0.2)       Carlsberg     30 (99.3)     55 (79.4)     48 (59.6)     39 (39.7)     27 (19.9)     11 (2.0)     5 (0.2)       Suss     81 (99.3)     67 (79.4)     57 (59.6)     41 (39.7)     29 (19.9)     19 (2.0)     11 (0.2)       Novo B     88 (99.3)     72 (79.4)     61 (59.6)     54 (39.7)     41 (19.9)     16 (2.0)     7 (0.2       Svendborg     108 (99.3)     98 (79.4)     84 (59.6)     73 (39.7)     57 (19.9)     22 (2.0)     9 (0.2)       Conditional Gauss	DS 1912		93 (79.4)	73 (59.6)	52 (39.7)	27 (19.9)	3 (2.0)	- (0.2)		
Svendborg     122 (99.3)     96 (79.4)     77 (59.6)     55 (39.7)     30 (19.9)     4 (2.0)     - (0.2)       Unconditional Gaussian method       95%     96%     97%     98%     99%     99.9%     99.99%       Portfolio     76 (99.3)     66 (79.4)     62 (59.6)     47 (39.7)     30 (19.9)     16 (2.0)     10 (0.2)       S&P 500     101 (159.9)     79 (127.9)     59 (95.9)     36 (64.0)     22 (32.0)     5 (3.2.)     3 (0.3)       B&O     61 (99.3)     55 (79.4)     48 (59.6)     39 (39.7)     27 (19.9)     11 (2.0)     5 (0.2)       DS 1912     105 (99.3)     95 (79.4)     85 (59.6)     67 (39.7)     48 (19.9)     19 (2.0)     11 (0.2)       Novo B     88 (99.3)     72 (79.4)     61 (59.6)     54 (39.7)     57 (19.9)     12 (2.0)     9 (0.2)       Seendborg     108 (99.3)     98 (79.4)     84 (59.6)     73 (39.7)     57 (19.9)     10 (2.0)     6 (0.2)       Swendborg     108 (99.3)     96 (79.4)     51 (59.6)     41 (39.7)     27 (19.9)	ISS	148 (99.3)	126 (79.4)	93 (59.6)	63 (39.7)	23 (19.9)	1 (2.0)	- (0.2)		
Unconditional Gaussian method       95%     96%     97%     98%     99%     99.9%     99.99%       Portfolio     76 (99.3)     66 (79.4)     62 (59.6)     47 (39.7)     30 (19.9)     16 (2.0)     10 (0.2       S&P 500     101 (159.9)     79 (127.9)     59 (95.9)     36 (64.0)     22 (32.0)     5 (32.2)     3 (0.3)       B&O     61 (99.3)     55 (79.4)     48 (59.6)     39 (39.7)     28 (19.9)     13 (2.0)     9 (0.2)       Carlsberg     63 (99.3)     55 (79.4)     85 (59.6)     67 (39.7)     48 (19.9)     19 (2.0)     11 (0.2)       Novo B     88 (99.3)     72 (79.4)     61 (59.6)     54 (39.7)     41 (19.9)     16 (2.0)     7 (0.2)       Swendborg     108 (99.3)     98 (79.4)     84 (59.6)     73 (39.7)     57 (19.9)     10 (2.0)     6 (0.2)       Ske P 500     151 (159.9)     127 (127.9)     88 (95.9)     61 (64.0)     33 (32.0)     7 (32.)     4 (0.3)       B&O     71 (99.3)     61 (79.4)     57 (59.6)     42 (39.7)     27 (19.9)     <	Novo B	113 (99.3)	90 (79.4)	70 (59.6)	49 (39.7)	26 (19.9)	2(2.0)	- (0.2)		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Svendborg	122 (99.3)	96 (79.4)	77 (59.6)	55 (39.7)	30 (19.9)	4 (2.0)	- (0.2)		
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $			Uncor	nditional Gaus	sian method					
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		95%	96%	97%	98%	99%	99.9%	99.99%		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Portfolio	76 (99.3)	66 (79.4)	62 (59.6)	47 (39.7)	30 (19.9)	16 (2.0)	10 (0.2)		
$ \begin{array}{c} \mbox{Carlsberg} & 63 (99.3) & 55 (79.4) & 48 (59.6) & 39 (39.7) & 27 (19.9) & 11 (2.0) & 5 (0.2 \\ \mbox{DS 1912} & 105 (99.3) & 95 (79.4) & 85 (59.6) & 67 (39.7) & 48 (19.9) & 19 (2.0) & 8 (0.2 \\ \mbox{ISS} & 81 (99.3) & 67 (79.4) & 57 (59.6) & 41 (39.7) & 29 (19.9) & 19 (2.0) & 11 (0.2 \\ \mbox{Novo B} & 88 (99.3) & 72 (79.4) & 61 (59.6) & 54 (39.7) & 41 (19.9) & 16 (2.0) & 7 (0.2 \\ \mbox{Svendborg} & 108 (99.3) & 98 (79.4) & 84 (59.6) & 73 (39.7) & 57 (19.9) & 22 (2.0) & 9 (0.2 \\ \mbox{Conditional Gaussian} \\ \hline \\ $	S&P 500							3 (0.3)		
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	B&O	61 (99.3)	56 (79.4)	49 (59.6)	40 (39.7)	28 (19.9)	13 (2.0)	9 (0.2)		
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	Carlsberg	63 (99.3)	55 (79.4)	48 (59.6)	39 (39.7)	27 (19.9)	11 (2.0)	5 (0.2)		
Novo B     88 (99.3)     72 (79.4)     61 (59.6)     54 (39.7)     41 (19.9)     16 (2.0)     7 (0.2       Svendborg     108 (99.3)     98 (79.4)     84 (59.6)     73 (39.7)     57 (19.9)     22 (2.0)     9 (0.2       Conditional Gaussian       Conditional Gaussian       95%     96%     97%     98%     99%     99.9%     99.99%       Portfolio     77 (99.3)     64 (79.4)     51 (59.6)     41 (39.7)     27 (19.9)     10 (2.0)     6 (0.2       S&P 500     151 (159.9)     127 (127.9)     88 (95.9)     61 (64.0)     33 (32.0)     7 (3.2)     4 (0.3       B&O     71 (99.3)     61 (79.4)     53 (59.6)     42 (39.7)     26 (19.9)     11 (2.0)     7 (0.2       DS 1912     90 (99.3)     53 (79.4)     44 (59.6)     36 (39.7)     23 (19.9)     9 (2.0)     4 (0.2       ISS     90 (98.2)     80 (78.6)     70 (58.9)     53 (39.3)     37 (19.6)     18 (2.0)     14 (0.2       Novo B     72 (99.3)     61 (79.4)     46 (59.6)     37 (39.	DS 1912		95 (79.4)	85 (59.6)	67 (39.7)	48 (19.9)	19 (2.0)	8 (0.2)		
Svendborg     108 (99.3)     98 (79.4)     84 (59.6)     73 (39.7)     57 (19.9)     22 (2.0)     9 (0.2       Conditional Gaussian       95%     96%     97%     98%     99%     99.9%     99.99%       Portfolio     77 (99.3)     64 (79.4)     51 (59.6)     41 (39.7)     27 (19.9)     10 (2.0)     6 (0.2       S&P 500     151 (159.9)     127 (127.9)     88 (95.9)     61 (64.0)     33 (32.0)     7 (3.2)     4 (0.3       B&O     71 (99.3)     61 (79.4)     53 (59.6)     42 (39.7)     27 (19.9)     11 (2.0)     7 (0.2       DS 1912     90 (99.3)     71 (79.4)     57 (59.6)     45 (39.7)     23 (19.9)     9 (2.0)     4 (0.2       ISS     90 (98.2)     80 (78.6)     70 (58.9)     53 (39.3)     37 (19.6)     18 (2.0)     14 (0.2       Novo B     72 (99.3)     61 (79.4)     46 (59.6)     37 (39.7)     24 (19.9)     8 (2.0)     3 (0.2       GEV and simple blocks estimator (95% threshold)       GEV and simple blocks estimator (95% threshold)	ISS	81 (99.3)	67 (79.4)	57 (59.6)	41 (39.7)	29 (19.9)	19 (2.0)	11 (0.2)		
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$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Svendborg	108 (99.3)	98 (79.4)	84 (59.6)	73 (39.7)	57 (19.9)	22 (2.0)	9 (0.2)		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			(	Conditional Ga	ussian					
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		95%	96%	97%	98%	99%	99.9%	99.99%		
B&O   71 (99.3)   61 (79.4)   53 (59.6)   42 (39.7)   27 (19.9)   11 (2.0)   7 (0.2     Carlsberg   60 (99.3)   53 (79.4)   44 (59.6)   36 (39.7)   26 (19.9)   11 (2.0)   5 (0.2     DS 1912   90 (99.3)   71 (79.4)   57 (59.6)   45 (39.7)   23 (19.9)   9 (2.0)   4 (0.2     ISS   90 (98.2)   80 (78.6)   70 (58.9)   53 (39.3)   37 (19.6)   18 (2.0)   14 (0.2     Novo B   72 (99.3)   61 (79.4)   46 (59.6)   37 (39.7)   24 (19.9)   8 (2.0)   3 (0.2     Svendborg   97 (99.3)   87 (79.4)   72 (59.6)   52 (39.7)   31 (19.9)   10 (2.0)   4 (0.2     GEV and simple blocks estimator (95% threshold)     GEV and simple blocks estimator (95% threshold)     See 96%   97%   98%   99%   99.9%   99.9%     S&P   43 (159.9)   37 (127.9)   25 (95.9)   15 (64.0)   8 (32.0)   2 (3.2)   1 (0.3)     B&O   54 (99.3)   46 (79.4)   34 (59.6)   23 (39.7)   8 (19.9)   0 (2.0)   0 (0.2)	Portfolio	77 (99.3)	64 (79.4)	51 (59.6)	41 (39.7)	27 (19.9)	10 (2.0)	6 (0.2)		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	S&P 500	151 (159.9)	127 (127.9)	88 (95.9)	61 (64.0)	33 (32.0)	7 (3.2)	4 (0.3)		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	B&O	71 (99.3)	61 (79.4)	53 (59.6)	42 (39.7)	27 (19.9)	11 (2.0)	7 (0.2)		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Carlsberg	60 (99.3)	53 (79.4)	44 (59.6)	36 (39.7)	26 (19.9)	11 (2.0)	5 (0.2)		
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Svendborg     97 (99.3)     87 (79.4)     72 (59.6)     52 (39.7)     31 (19.9)     10 (2.0)     4 (0.2)       GEV and simple blocks estimator (95% threshold)       95%     96%     97%     98%     99%     99.9%     99.99%       Portfolio     71 (99.3)     57 (79.4)     36 (59.6)     19 (39.7)     11 (19.9)     0 (2.0)     0 (0.2)       S&P     43 (159.9)     37 (127.9)     25 (95.9)     15 (64.0)     8 (32.0)     2 (3.2)     1 (0.3)       B&O     54 (99.3)     46 (79.4)     34 (59.6)     23 (39.7)     8 (19.9)     0 (2.0)     0 (0.2)       Carlsberg     40 (99.3)     33 (79.4)     24 (59.6)     16 (39.7)     7 (19.9)     0 (2.0)     0 (0.2)       DS 1912     66 (99.3)     55 (79.4)     44 (59.6)     28 (39.7)     14 (19.9)     1 (2.0)     0 (0.2)       ISS     79 (99.1)     60 (79.3)     36 (59.5)     20 (39.6)     11 (19.8)     0 (2.0)     0 (0.2)	ISS	90 (98.2)	80 (78.6)	70 (58.9)	53 (39.3)	37 (19.6)	18 (2.0)	14 (0.2)		
GEV and simple blocks estimator (95% threshold)       95%     96%     97%     98%     99%     99.9%     99.99%       Portfolio     71 (99.3)     57 (79.4)     36 (59.6)     19 (39.7)     11 (19.9)     0 (2.0)     0 (0.2)       S&P     43 (159.9)     37 (127.9)     25 (95.9)     15 (64.0)     8 (32.0)     2 (3.2)     1 (0.3)       B&O     54 (99.3)     46 (79.4)     34 (59.6)     23 (39.7)     8 (19.9)     0 (2.0)     0 (0.2)       Carlsberg     40 (99.3)     33 (79.4)     24 (59.6)     16 (39.7)     7 (19.9)     0 (2.0)     0 (0.2)       DS 1912     66 (99.3)     55 (79.4)     44 (59.6)     28 (39.7)     14 (19.9)     1 (2.0)     0 (0.2)       ISS     79 (99.1)     60 (79.3)     36 (59.5)     20 (39.6)     11 (19.8)     0 (2.0)     0 (0.2)	Novo B	72 (99.3)	61 (79.4)	46 (59.6)	37 (39.7)	24 (19.9)	8 (2.0)	3 (0.2)		
95%     96%     97%     98%     99%     99.9%     99.9%     99.99%       Portfolio     71 (99.3)     57 (79.4)     36 (59.6)     19 (39.7)     11 (19.9)     0 (2.0)     0 (0.2)       S&P     43 (159.9)     37 (127.9)     25 (95.9)     15 (64.0)     8 (32.0)     2 (3.2)     1 (0.3)       B&O     54 (99.3)     46 (79.4)     34 (59.6)     23 (39.7)     8 (19.9)     0 (2.0)     0 (0.2)       Carlsberg     40 (99.3)     33 (79.4)     24 (59.6)     16 (39.7)     7 (19.9)     0 (2.0)     0 (0.2)       DS 1912     66 (99.3)     55 (79.4)     44 (59.6)     28 (39.7)     14 (19.9)     1 (2.0)     0 (0.2)       ISS     79 (99.1)     60 (79.3)     36 (59.5)     20 (39.6)     11 (19.8)     0 (2.0)     0 (0.2)	Svendborg	97 (99.3)	87 (79.4)	72 (59.6)	52 (39.7)	31 (19.9)	10 (2.0)	4 (0.2)		
Portfolio71 (99.3)57 (79.4)36 (59.6)19 (39.7)11 (19.9)0 (2.0)0 (0.2)S&P43 (159.9)37 (127.9)25 (95.9)15 (64.0)8 (32.0)2 (3.2)1 (0.3)B&O54 (99.3)46 (79.4)34 (59.6)23 (39.7)8 (19.9)0 (2.0)0 (0.2)Carlsberg40 (99.3)33 (79.4)24 (59.6)16 (39.7)7 (19.9)0 (2.0)0 (0.2)DS 191266 (99.3)55 (79.4)44 (59.6)28 (39.7)14 (19.9)1 (2.0)0 (0.2)ISS79 (99.1)60 (79.3)36 (59.5)20 (39.6)11 (19.8)0 (2.0)0 (0.2)			GEV and simpl	e blocks estin	nator (95% thr	eshold)				
S&P43 (159.9)37 (127.9)25 (95.9)15 (64.0)8 (32.0)2 (3.2)1 (0.3)B&O54 (99.3)46 (79.4)34 (59.6)23 (39.7)8 (19.9)0 (2.0)0 (0.2)Carlsberg40 (99.3)33 (79.4)24 (59.6)16 (39.7)7 (19.9)0 (2.0)0 (0.2)DS 191266 (99.3)55 (79.4)44 (59.6)28 (39.7)14 (19.9)1 (2.0)0 (0.2)ISS79 (99.1)60 (79.3)36 (59.5)20 (39.6)11 (19.8)0 (2.0)0 (0.2)		95%	96%	97%	98%	99%	99.9%	99.99%		
S&P43 (159.9)37 (127.9)25 (95.9)15 (64.0)8 (32.0)2 (3.2)1 (0.3)B&O54 (99.3)46 (79.4)34 (59.6)23 (39.7)8 (19.9)0 (2.0)0 (0.2)Carlsberg40 (99.3)33 (79.4)24 (59.6)16 (39.7)7 (19.9)0 (2.0)0 (0.2)DS 191266 (99.3)55 (79.4)44 (59.6)28 (39.7)14 (19.9)1 (2.0)0 (0.2)ISS79 (99.1)60 (79.3)36 (59.5)20 (39.6)11 (19.8)0 (2.0)0 (0.2)	Portfolio	71 (99.3)	57 (79.4)	36 (59.6)	19 (39.7)	11 (19.9)	0 (2.0)	0 (0.2)		
Carlsberg40 (99.3)33 (79.4)24 (59.6)16 (39.7)7 (19.9)0 (2.0)0 (0.2)DS 191266 (99.3)55 (79.4)44 (59.6)28 (39.7)14 (19.9)1 (2.0)0 (0.2)ISS79 (99.1)60 (79.3)36 (59.5)20 (39.6)11 (19.8)0 (2.0)0 (0.2)	S&P	43 (159.9)	37 (127.9)	25 (95.9)	15 (64.0)	8 (32.0)	2 (3.2)	1 (0.3)		
DS 1912     66 (99.3)     55 (79.4)     44 (59.6)     28 (39.7)     14 (19.9)     1 (2.0)     0 (0.2)       ISS     79 (99.1)     60 (79.3)     36 (59.5)     20 (39.6)     11 (19.8)     0 (2.0)     0 (0.2)	B&O	54 (99.3)	46 (79.4)	34 (59.6)	23 (39.7)	8 (19.9)	0 (2.0)	0 (0.2)		
ISS 79 (99.1) 60 (79.3) 36 (59.5) 20 (39.6) 11 (19.8) 0 (2.0) 0 (0.2)	Carlsberg	40 (99.3)	33 (79.4)	24 (59.6)	16 (39.7)	7 (19.9)	0 (2.0)	0 (0.2)		
	DS 1912	66 (99.3)	55 (79.4)	44 (59.6)	28 (39.7)	14 (19.9)	1 (2.0)	0 (0.2)		
Novo B 62 (99.3) 54 (79.4) 40 (59.6) 26 (39.7) 11 (19.9) 1 (2.0) 0 (0.2)	ISS	79 (99.1)	60 (79.3)	36 (59.5)	20 (39.6)	11 (19.8)	0 (2.0)	0 (0.2)		
	Novo B	62 (99.3)	54 (79.4)	40 (59.6)	26 (39.7)	11 (19.9)	1 (2.0)	0 (0.2)		

Svendborg

77 (99.3)

67 (79.4)

54 (59.6)

34 (39.7)

12(19.9)

1(2.0)

0(0.2)

# Backtesting

 compute VaR from the first six years of data, see if it "is violated", i.e. if next days return is lower than VaR, repeat again using six years of data but starting one day later, two days later, ... count number of violations

# expected no. of violations in parentheses

			results, violatio				
		GEV and simpl	e blocks estima	tor (99% three	shold)		
	95%	96%	97%	98%	99%	99.9%	99.99%
Portfolio	140 (99.3)	106 (79.4)	78 (59.6)	56 (39.7)	17 (19.9)	1(2.0)	0 (0.2)
S&P500	79 (159.9)	56 (127.9)	36 (95.9)	25 (64.0)	13 (32.0)	2 (3.2)	2 (0.3)
B&O	80 (99.3)	63 (79.4)	51 (59.6)	38 (39.7)	15 (19.9)	0 (2.0)	0 (0.2)
Carlsberg	80 (99.3)	70 (79.4)	51 (59.6)	33 (39.7)	16 (19.9)	0(2.0)	0 (0.2)
DS 1912	108 (99.3)	94 (79.4)	75 (59.6)	48 (39.7)	23 (19.9)	4 (2.0)	0 (0.2)
ISS	157 (99.1)	129 (79.3)	97 (59.5)	61 (39.6)	23 (19.8)	2 (2.0)	0 (0.2)
Novo B	115 (99.3)	93 (79.4)	71 (59.6)	49 (39.7)	25 (19.9)	2 (2.0)	0 (0.2)
Svendborg	125 (99.3)	106 (79.4)	82 (59.6)	60 (39.7)	26 (19.9)	3 (2.0)	0 (0.2)
		GEV and bl	ocks estimator	(95% threshol	d)		
	95%	96%	97%	98%	99%	99.9%	99.99%
Portfolio	139 (99.3)	107 (79.4)	78 (59.6)	54 (39.7)	18 (19.9)	1 (2.0)	0 (0.2)
S&P500	97 (159.9)	75 (127.9)	57 (95.9)	34 (64.0)	15 (32.0)	3 (3.2)	2 (0.3)
B&O	89 (99.3)	73 (79.4)	58 (59.6)	44 (39.7)	17 (19.9)	1(2.0)	0 (0.2)
Carlsberg	77 (99.3)	65 (79.4)	46 (59.6)	33 (39.7)	14 (19.9)	0 (2.0)	0 (0.2)
DS 1912	112 (99.3)	90 (79.4)	70 (59.6)	49 (39.7)	21 (19.9)	3 (2.0)	0 (0.2)
ISS	147 (99.1)	129 (79.3)	94 (59.5)	46 (39.6)	20 (19.8)	1(2.0)	0 (0.2)
Novo B	109 (99.3)	88 (79.4)	65 (59.6)	45 (39.7)	21 (19.9)	2 (2.0)	0 (0.2)
Svendborg	118 (99.3)	100 (79.4)	80 (59.6)	58 (39.7)	29 (19.9)	2 (2.0)	0 (0.2)
		GEV and bl	ocks estimator	(99% threshol	d)		
	95%	96%	97%	98%	99%	99.9%	99.99%
Portfolio	166 (99.3)	133 (79.4)	99 (59.6)	62 (39.7)	23 (19.9)	1 (2.0)	0 (0.2)
S&P500	88 (159.9)	66 (127.9)	45 (95.9)	31 (64.0)	14 (32.0)	3 (3.2)	2 (0.3)
B&O	86 (99.3)	75 (79.4)	59 (59.6)	45 (39.7)	18 (19.9)	1(2.0)	0 (0.2)
Carlsberg	102 (99.3)	78 (79.4)	61 (59.6)	42 (39.7)	20 (19.9)	0(2.0)	0 (0.2)
DS 1912	126 (99.3)	104 (79.4)	87 (59.6)	55 (39.7)	27 (19.9)	5 (2.0)	1(0.2)
ISS	187 (99.1)	156 (79.3)	114 (59.5)	75 (39.6)	27 (19.8)	2 (2.0)	0 (0.2)
Novo B	133 (99.3)	109 (79.4)	81 (59.6)	58 (39.7)	30 (19.9)	4 (2.0)	0 (0.2)
Svendborg	144 (99.3)	121 (79.4)	99 (59.6)				
			GPD				
	95%	96%	97%	98%	99%	99.9%	99.99%
Portfolio	118 (99.3)	98 (79.4)	78 (59.6)	57 (39.7)	20 (19.9)	1(2.0)	0 (0.2)
S&P500	26 (20.8)	26 (16.6)	21 (12.5)	16 (8.32)	5 (4.1)	2 (0.4)	1 (0.04
B&O	89 (98.9)	74 (79.1)	54 (59.3)	38 (39.5)	16 (19.8)	2 (2.0)	0 (0.2)
Carlsberg	69 (95.6)	56 (76.8)	46 (57.6)	33 (38.4)	16 (19.2)	1 (2.0)	0 (0.2)
DS 1912	98 (74.3)	76 (59.4)	65 (44.6)	41 (29.7)	24 (14.9)	4 (1.5)	1(0.1)
ISS	151 (99.3)	128 (79.4)	95 (59.6)	61 (39.7)	26 (19.9)	3 (2.0)	0 (0.2)
Novo B	116 (99.2)	89 (79.4)	70 (59.5)	50 (39.7)	27 (19.8)	4 (2.0)	1 (0.2)
Svendborg	110 (88.9)	96 (71.1)	68 (53.3)	52 (35.5)	25 (17.8)	4 (1.8)	0 (0.2)

# Backtesting

 compute VaR from the first six years of data, see if it "is violated", i.e. if next days return is lower than VaR, repeat again using six years of data but starting one day later, two days later, ... count number of violations

• expected no. of

violations in parentheses

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		Backtesting GARCH based	results, violat: extreme value	•			
	95%	96%	97%	98%	99%	99.9%	99.99%
Portfolio	109 (99.3)	91 (79.4)	64 (59.6)	44 (39.7)	18 (19.9)	1(2.0)	0 (0.2)
S&P 500	145 (157.8)	123 (126.2)	88 (94.7)	60 (63.1)	34 (31.6)	6 (3.2)	2 (0.3)
B&O	95 (99.3)	73 (79.4)	53 (59.6)	33 (39.7)	12 (19.9)	2 (2.0)	0 (0.2)
Carlsberg	75 (99.3)	61 (79.4)	45 (59.6)	32 (39.7)	20 (19.9)	0 (2.0)	0 (0.2)
DS 1912	94 (98.3)	66 (78.6)	48 (59.0)	26 (39.3)	11 (19.6)	2(2.0)	1 (0.2)
ISS	144 (98.2)	117 (78.5)	87 (58.9)	57 (39.3)	22 (19.6)	5 (2.0)	0 (0.2)
Novo B	93 (99.3)	75 (79.4)	52 (59.6)	36 (39.7)	18 (19.9)	2(2.0)	0 (0.2)
Svendborg	102 (99.3)	87 (79.4)	60 (59.6)	34 (39.7)	14 (19.9)	3 (2.0)	1 (0.2)
		GARCH based e	extreme value	method, unco	nditional		
	95%	96%	97%	98%	99%	99.9%	99.99%
Portfolio	107 (98.1)	90 (78.4)	66 (58.8)	44 (39.2)	16 (19.6)	0 (2.0)	0 (0.2)
S&P500	98 (143.8)	77 (115.1)	55 (86.3)	30 (57.5)	14 (28.8.0)	2 (2.9)	0 (0.3)
B&O	82 (99.3)	65 (79.4)	52 (59.6)	34 (39.7)	14 (19.9)	0(2.0)	0 (0.2)
Carlsberg	88 (98.8)	77 (79.0)	62 (59.3)	37 (39.5)	22 (19.8)	0 (2.0)	0 (0.2)
DS 1912	108 (94.8)	87 (75.8)	69 (56.9)	43 (37.9)	20 (19.0)	1(2.0)	0 (0.2)
ISS	114 (81.7)	100 (65.3)	70 (49.0)	41 (32.7)	16 (16.3)	1 (1.6)	0 (0.2)
Novo B	106 (99.2)	87 (79.4)	62 (59.5)	49 (39.7)	25 (19.8)	2 (2.0)	0 (0.2)
Svendborg	115 (98.6)	100 (78.8)	76 (59.1)	56 (39.4)	27 (19.7)	2(2.0)	0 (0.2)

# Backtesting

• compute VaR from the first six years of data, see if it "is violated", i.e. if next days return is lower than VaR, repeat again using six years of data but starting one day later, two days later, ... count number of violations

• expected no. of violations in parentheses

## A final important reminder

For a stationary sequence block maxima (of course) are stochastically larger than one-day values, and block maxima over longer blocks are stochastically larger than maxima over shorter blocks.

(That a random variable is stochastically larger than another one means that it's distribution function lies to the right of the other one. Think carefully through what this means practically and why it is true)

Always make plots of your data/time series. This makes it possible to see if your results and choices are OK/good



Why is this picture here? Try to understand why.