

7.3 Assume the neutrino has mass m_ν and that is the whole reason it arrives 2 h late
(It is not. There are also stellar astrophysical processes involved.).

For the neutrino: $\gamma = \frac{E}{m_\nu c^2}$

$$\Rightarrow v = \sqrt{1 - \frac{m_\nu^2 c^4}{E^2}} c \approx // \text{Taylor} // \left(1 - \frac{m_\nu^2 c^4}{2E^2}\right) c$$

The time difference between the arrival of the ν and the photon is

$$\Delta t = \frac{L}{v} - \frac{L}{c} \approx // \text{Taylor} //$$

$$= \frac{L}{c} \left(1 + \frac{m_\nu^2 c^4}{2E^2}\right) - \frac{L}{c} = \frac{L m_\nu^2 c^3}{2E^2}$$

$$\Rightarrow m_\nu = \sqrt{\frac{2E^2 \Delta t}{L c^3}} = \frac{E}{c^2} \sqrt{\frac{2 \Delta t c}{L}}$$

$$= 20 \text{ MeV} / c^2 \cdot \sqrt{\frac{2 \times 2.8 \times 10^8 \times 365 \times 24 \times 60 \times 60}{1.68 \times 10^5}}$$

$$= 20 \text{ MeV}/c^2 \times 5.2 \times 10^{-5} = 1.04 \text{ keV}/c^2.$$

Note that this is NOT the strongest bound on the ν mass we have !